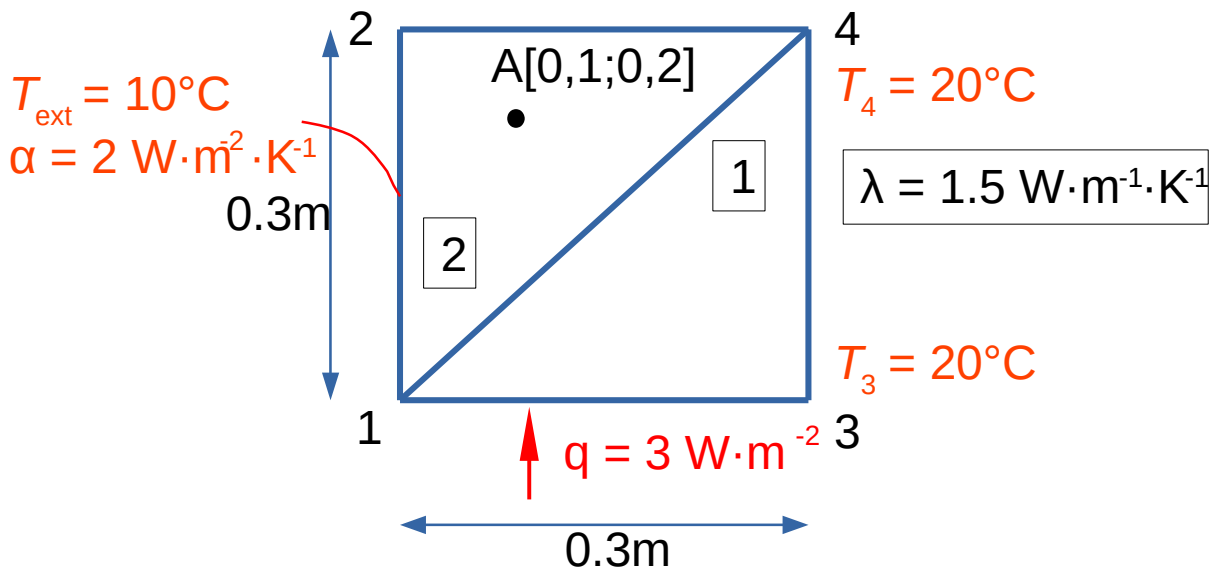
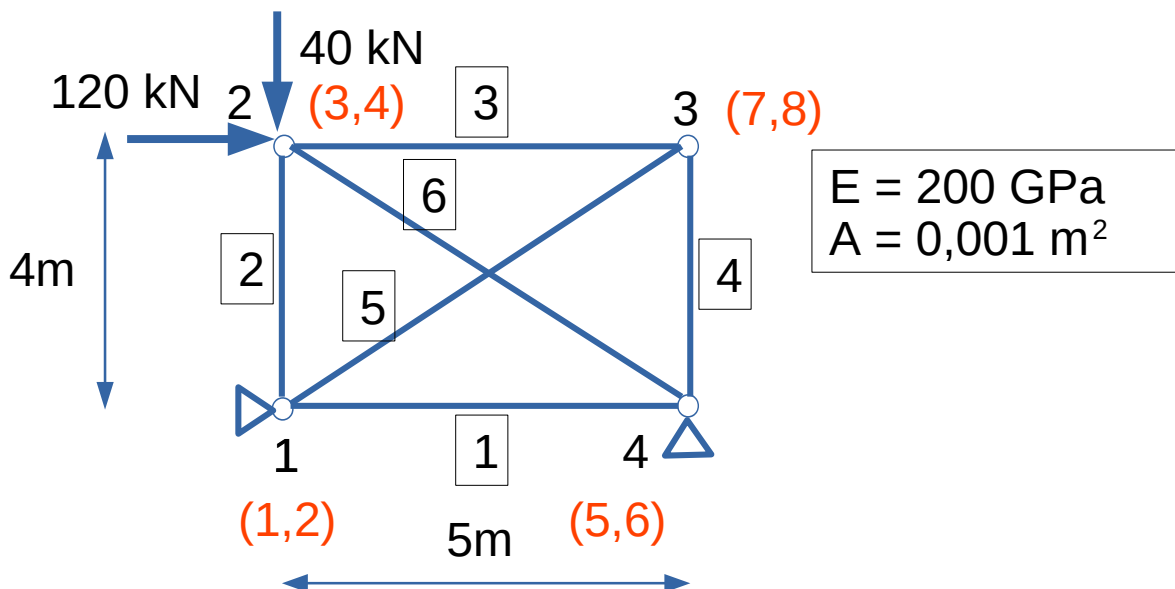


Final exam – Numerical analysis of structures

- 1) a) Determine temperatures at all nodes for 2D heat transfer problem - steady state.
b) Determine temperature at point A for given temperatures $T_1 = 10^\circ\text{C}$ and $T_2 = 15^\circ\text{C}$, $T_4 = 10^\circ\text{C}$.

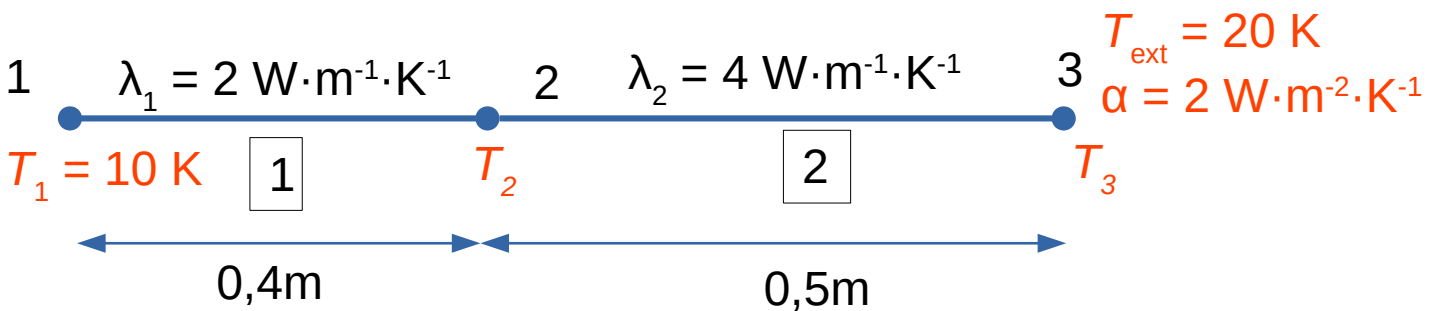


- 2) a) Determine the 5th row of the stiffness matrix for the truss structure.
b) Determine the right-hand side vector for:
 - force loading
 - prescribed displacement $u_3 = 1\text{mm}$
 - temperature loading (uniform temperature change) of bar No. 5
 $\Delta T = 10^\circ\text{C}$, $\alpha = 12 \cdot 10^{-6} \text{ K}^{-1}$
- c) Determine the axial force of bar No. 6 for given displacements $u_2 = -0.002\text{m}$ and $v_2 = 0.0005\text{m}$.



Final exam – Numerical analysis of structures

- 3) 1D heat transfer problem – non-stationary problem:
- Determine the temperature profile in steady state.
 - Calculate nodal temperatures for the first two time steps t_1 and t_2 in the time-dependent problem (non-stationary). For time discretization, use the finite difference method with $\Delta t = 1\text{s}$, $\rho = 10$, $c = 1$, $\tau = \frac{1}{2}$. The initial temperature is $t_0 = 10\text{ K}$.



- 4) The wall is discretized by two triangle elements (thickness $h=0,4\text{ m}$). Determine:
- both displacements at node No. 4 (horizontal u_{4x} and vertical u_{4y})
 - strain vector at point A for given displacements:

$$u_{1x} = u_{1y} = u_{3y} = 0; u_{3x} = 1\text{mm}, u_{4x} = 2\text{mm}, u_{4y} = -0,5\text{mm}$$

